

SCIO 2015

$$1) M = 1^2 + 2^2 + 3^2 = 14$$

$$N = 1 + 2 + 3 = 6$$

$$M - N = 8 \Rightarrow \textcircled{C}$$

$$2) 2(x-3)^2 - k = (x-2)^2$$

$$2(x^2 - 6x + 9) - k = x^2 - 4x + 4$$

$$2x^2 - 12x + 18 - k = x^2 - 4x + 4$$

$$x^2 - 8x + 14 = k \Rightarrow \textcircled{A}$$

3) Použijeme vzorec $(m-2) \cdot 180^\circ = \text{výšekdlo} \dots m \text{ je počet vrcholních úhlů}$

$$x = (8-2) \cdot 180^\circ = 1080^\circ \Rightarrow \textcircled{D}$$

4) Původní cena .. 10 000,- Kč

Cena po zdražení .. 12 000,- Kč

Cena po slevě .. $\frac{3}{4}$ z původní ceny = 4 500,-

$$\begin{array}{r} \uparrow 100\% \dots 12\,000,- \uparrow \\ \hline x\% \dots 4\,500,- \end{array}$$

$$\frac{x}{100} = \frac{4500}{12000} \Rightarrow x = \frac{4500 \cdot 100}{12000} = 62,5\% \Rightarrow \textcircled{B}$$

5) $\frac{2}{5}$ nákupu vzdily 2 kg

$\frac{5}{5}$ nákupu (celý nákup) vzdely 5 kg $\Rightarrow \textcircled{C}$

$$6) S_{\square} = a^2 = 2^2 = 4 \text{ m}^2$$

$$S_{\circ} = \pi r^2 = 3,14 \cdot 1^2 = 3,14 \text{ m}^2$$

$$S_{\text{celková}} = 4 - 3,14 = 0,86 \text{ m}^2 \Rightarrow \textcircled{B}$$

$$7) 600 \cdot 25 = 15000,- \text{ Kč}$$

$$2\% z 15000,- = 300,- \text{ Kč}$$

$$15000 + 300 = 15300,- \Rightarrow \textcircled{C}$$

$$8) (-x+2y)^2 = x^2 - 4xy + 4y^2 \Rightarrow \textcircled{D}$$

9) Obecna:

- a) Délka stánuč uhloprícty v krychli je $a \cdot \sqrt{2}$ (a je délka hrany krychle)
 b) -II- tělesové uhloprícty -II- $a \cdot \sqrt{3}$

Výsledek: $6\sqrt{3} \Rightarrow \textcircled{B}$

10)

$$\begin{aligned} 1.\text{syn} &\dots \frac{1}{2}x \\ 2.\text{syn} &\dots \frac{1}{2} \cdot \frac{1}{2}x = \frac{1}{4}x \quad \left. \right\} \frac{3}{4}x \\ 3.\text{syn} &\dots \cancel{\frac{1}{2}\cancel{\frac{1}{2}\cancel{\frac{1}{2}\cancel{\frac{1}{2}\cancel{\frac{1}{2}}}}}x} = \frac{1}{8}x \quad \left. \right\} \frac{7}{8}x \\ 4.\text{syn} &\dots \cancel{\frac{1}{2}\cancel{\frac{1}{2}\cancel{\frac{1}{2}\cancel{\frac{1}{2}\cancel{\frac{1}{2}}}}}x} = \frac{1}{16}x \\ 5.\text{syn} &\dots \boxed{\frac{1}{16}x} \Rightarrow \textcircled{B} \\ \text{Dohrad} &\dots x \end{aligned}$$

11)

$$\begin{array}{rcl} \downarrow 5 \text{ dělky} & \dots & 15 \text{ dlu}^{\circ} \uparrow \\ \hline \downarrow 3 \text{ dělky} & \dots & x \text{ dlu}^{\circ} \uparrow \\ \hline \frac{x}{15} = \frac{5}{3} & \Rightarrow x = \frac{5 \cdot 15}{3} = 25 \text{ dlu}^{\circ} & \Rightarrow \textcircled{C} \end{array}$$

12)

$\frac{1}{a} < \frac{1}{b}$... Je-li $a > b$, pot pøevrácené hodnoty mají opaènou smyslnost nevìrovnosti. Zbytek odpovídá OVEŘTE (napøíklad 1 příklad, kdy to neplatí).

13)

$\textcircled{A} \rightarrow$ mì kružnice \rightarrow 2 tescny
 na kružnici \rightarrow 1 tescny
 urvití \rightarrow 0 tescny



} provéde konstrukci tescen do obrazku (napøíklad Thalesov kružnici)

14)

$\textcircled{A} \rightarrow y = -x + 2$; $A[-1, 1] \Rightarrow 1 \neq -(-1) + 2$
 $1 \neq 3 \Rightarrow \text{NELEZE}$

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15) $1+3+2=6$ díly \dots 30 pr.

1 díl \dots 5 príkloù

Arithmetika \Rightarrow 3 díly \dots 15 príkloù $\Rightarrow \textcircled{C}$

16)



$$a^2 = 4^2 + 3^2$$

$$a^2 = 25$$

$$a = 5 \text{ cm}$$

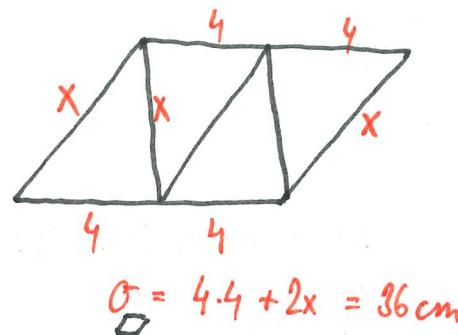
$$\sigma = 4 \cdot 5 = 20 \text{ cm} \Rightarrow \textcircled{D}$$

$$\begin{aligned} 4 \cdot 12 &= 48 \text{ místků} \\ 48 \cdot 600 &= 28800,- \\ \uparrow 100\% &\dots 20000,- \uparrow \\ x\% &\dots 28800 \\ x &= 144\% \Rightarrow 0.44\% \Rightarrow \textcircled{B} \end{aligned}$$

$$18) 5 - 3(-1-1) + 2(-1-2)^2 = 5 + 6 + 18 = 29 \Rightarrow \textcircled{D}$$

$$19) 2x = 36 - 4 \cdot 4 = 20 \text{ cm} \\ x = 10 \text{ cm}$$

$$O = 4+10+10 = 24 \text{ cm} \Rightarrow \textcircled{D}$$



$$20) \begin{array}{l} \text{Jablko} \dots 12 \text{ Kč} \\ \text{Hruška} \dots 8 \text{ Kč} \\ \text{Pomaranč} \dots 4 \text{ Kč} \\ \text{Banán} \dots 8 \text{ Kč} \end{array} \quad \underline{\quad 32 \text{ Kč}} \Rightarrow \textcircled{C}$$

$$21) 2x + \frac{1}{3}y = 3+y \quad | \cdot 3$$

$$\frac{x+y}{2} = \frac{1}{4}x - \frac{11}{8} \quad | \cdot 8$$

$$6x + y = 9 + 3y$$

$$4x + 4y = 2x - 11$$

$$6x - 2y = 9 \quad | \cdot 2$$

$$2x + 4y = -11$$

$$12x - 4y = 18 \quad | \cdot 2$$

$$2x + 4y = -11 \quad | +$$

$$14x = 4$$

$$x = \frac{1}{2} \Rightarrow y = -3 \Rightarrow \textcircled{B}$$

$$22) \frac{a-2b}{5c-2} = \frac{-1-2 \cdot \frac{11}{4}}{\frac{5 \cdot 2 - 2}{6-2}} = \frac{-1-2 \cdot \frac{11}{4}}{\frac{8}{-3}} = \frac{-1-\frac{11}{2}}{\frac{8}{-3}} = \frac{-\frac{13}{2}}{-\frac{3}{4}} = \frac{\frac{13}{2} \cdot \frac{4}{3}}{\frac{13}{12}} = \frac{13}{12} \Rightarrow$$

$$b = 2 \cdot \frac{3}{4} = \frac{11}{4}$$

\Rightarrow řešení je odpověď není správná

$$a-2b = -1-2 \cdot \frac{11}{4} = -1 - \frac{22}{4} = -\frac{26}{4} = -\frac{13}{2}$$

$$23) V = 8 \cdot 3 \cdot 1,5 \text{ m}^3 = 36 \text{ m}^3 = 36000 \text{ l}$$

$$x = \frac{36000}{60} : 15 = 2400 \text{ s} = 40 \text{ minut} \Rightarrow \textcircled{C}$$

$$24) \frac{x+2}{4} - \frac{2-x}{2} = x-2 \quad | \cdot 4$$

$$x+2 - 2(2-x) = 4x-8$$

$$x+2 - 4 + 2x = 4x-8$$

$$\begin{aligned} -x &= -6 \\ x &= 6 \Rightarrow \textcircled{D} \end{aligned}$$

$$25) 1\text{cm na mapě} = 450000\text{ cm re skutečnosti} \\ = 4500\text{ m} \quad \text{--} \\ = 4,5\text{ km} \quad \text{--}$$

$$2\text{dm} = 20\text{cm na mapě} = 20 \cdot 4500\text{m} = 90000\text{m}$$

$$x = 90000 : 5 = 18000\text{s} = 5\text{ hodin}$$

$$10h + 5h = 15h \Rightarrow \textcircled{C}$$

$$26) K_1 = \frac{1}{2} \cdot 6 = 3\text{cm} = 30\text{mm}$$

$$O_1 = 2\pi r_1 = 2\pi \cdot 30 = 60\pi\text{ mm} = 6\pi\text{ cm}$$

$$K_2 = 30 - \frac{1}{2} \cdot 20 = 20\text{ mm}$$

$$O_2 = 2\pi r_2 = 40\pi\text{ mm} = 4\pi\text{ cm}$$

$$\left. \begin{array}{l} \text{z Mapoučího} \\ O = 2\pi\text{ cm} = 6,28\text{ cm} \end{array} \right\} \Rightarrow \textcircled{D}$$

$$27) \textcircled{C} \rightarrow 41957 \cancel{4} - \text{jednotka} 2 \\ = -\text{jednotka} 3 \Rightarrow \text{jednotka} \underline{\underline{6}}$$

$$28) \frac{9x^2-y^2}{y^2-3x^2} : \frac{3x+y}{x^2y} = \frac{(3x-y)(3x+y)}{x^2(y-3x)} \cdot \frac{x^2y}{3x+y} = \frac{(3 \cdot 3 - (-2))}{(-2 - 3 \cdot 3)} \cdot \frac{1(-2)}{1} = \frac{11}{-11} \cdot \frac{(-2)}{1} = 2 \Rightarrow \textcircled{C}$$

$$29)$$

$$\begin{aligned} r^2 &= 5^2 - 3^2 = 16 \\ r &= 4\text{ cm} \\ s &= \frac{r \cdot R}{2} \\ S &= \frac{6 \cdot 4}{2} \text{ cm}^2 = 12\text{ cm}^2 \Rightarrow \textcircled{D} \end{aligned}$$

$$30) \frac{x+220}{5} - 100 = x \quad | \cdot 5$$

$$x+220 - 500 = 5x$$

$$-280 = 4x$$

$$x = -40 \Rightarrow \textcircled{B}$$